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SOFTWARE SET-VALUE PROFILING AND CODE REUSE

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SOFTWARE SET-VALUE PROFILING AND CODE REUSE

- Field**
- 5 The present invention relates generally to software, and more specifically to
software capable of reusing regions of code.

Background of the Invention

- Modern software programs include many instructions that are executed
10 multiple times each time the program is executed. Typically, large programs have
logical “regions” of instructions, each of which may be executed many times. When
a region is one that is executed more than once, and the results produced by the
region are the same for more than one execution, the region is a candidate for
“reuse.” The term “reuse” refers to the reusing of results from a previous execution
15 of the region.

- For example, a computation reuse region could be a region of software
instructions that, when executed, read a first set of registers and modify a second set
of registers. The data values in the first set of registers are the “inputs” to the
computation reuse region, and the data values deposited into the second set of
20 registers are the “results” of the computation reuse region. A buffer holding inputs
and results can be maintained for the region. Each entry in the buffer is termed an
“instance.” When the region is encountered during execution of the program, the
buffer is consulted and if an instance with matching input values is found, the results
can be used without having to execute the software instructions in the computation
25 reuse region. When reusing the results is faster than executing the software
instructions in the region, performance improves. Such a buffer is described in:
Daniel Connors & Wen-mei Hwu, “Compiler-Directed Dynamic Computation
Reuse: Rationale and Initial Results,” Proceedings of the 32nd Annual International
Symposium on Microarchitecture (MICRO), November 1999.
30 Some regions make better candidates for reuse than others. For example, a
region capable of producing an often-reused instance is a good candidate for reuse.

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In contrast, regions that produce instances that are not reused often generally do not make good candidates for reuse, in part because new instances are frequently generated, and buffered instances are not often reused. Regions that are candidates for reuse are typically identified when the program is compiled. The compiler

- 5 identifies candidates for reuse, and selects which candidates are to be computation reuse regions after the program is compiled. This can be a difficult problem, in part because the compiler does not necessarily have information describing whether candidate regions have the qualities that make for good reuse regions.

Some compilers use value profiling algorithms in an attempt to identify
10 variables with invariant behavior. One such value profiling algorithm is discussed in: Brad Calder, Peter Feller & Alan Eustace, "Value Profiling," Proceedings of the 30th Annual International Symposium on Microarchitecture (MICRO), December 1997. Calder et al. present a technique that attempts to identify variables with invariant behavior by observing each variable accessed by instructions. Calder et al.
15 also present a technique that observes each variable for a period of time and then tests for convergence. This approach can incur significant overhead, in part because every value generated by every instruction is profiled. Value profiling as described by Calder et al. is not directly applicable to the identification of reuse regions, in part because regions often have inputs and outputs that include multiple variables.

20 For the reasons stated above, and for other reasons stated below which will become apparent to those skilled in the art upon reading and understanding the present specification, there is a need in the art for an alternate method and apparatus for identifying and profiling candidate reuse regions.

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Brief Description of the Drawings

Figure 1 shows a candidate reuse region;

Figure 2 shows input values and set-values for the candidate reuse region of Figure 1;

30 Figure 3A shows a set-value in accordance with one embodiment of the invention;

Figure 3B shows a set-value in accordance with another embodiment of the invention;

Figure 4 shows a profiling data structure;

Figure 5A shows a sampling value profiler;

5 Figure 5B shows instrumenting code that implements the sampling value profiler of Figure 5A;

Figure 6A shows software instructions that access an array;

Figure 6B shows a location-value in accordance with one embodiment of the present invention;

10 Figure 6C shows a location-value in accordance with another embodiment of the present invention;

Figure 6D shows a location-value profiling data structure;

Figure 7 shows a flowchart for a method of selecting reuse regions; and

Figure 8 shows a processing system.

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Description of Embodiments

In the following detailed description of the embodiments, reference is made to the accompanying drawings that show, by way of illustration, specific embodiments in which the invention may be practiced. In the drawings, like numerals describe substantially similar components throughout the several views. These embodiments are described in sufficient detail to enable those skilled in the art to practice the invention. Other embodiments may be utilized and structural, logical, and electrical changes may be made without departing from the scope of the present invention. Moreover, it is to be understood that the various embodiments of the invention, although different, are not necessarily mutually exclusive. For example, a particular feature, structure, or characteristic described in one embodiment may be included within other embodiments. The following detailed description is, therefore, not to be taken in a limiting sense, and the scope of the present invention is defined only by the appended claims, along with the full scope of equivalents to which such claims are entitled.

- The method and apparatus of the present invention provide a profiling mechanism useful for forming computation reuse regions from a list of candidate reuse regions. A computation reuse region has a number of input registers. Values held in the input registers are input values to the region when the region is executed.
- 5 When the input registers for a candidate reuse region only take on a few sets of different values, the candidate reuse region can be profitably reused. Each set of different values, hereinafter referred to as “set-values,” corresponds generally to a reuse instance that will be generated at runtime. Candidate reuse regions exhibiting this behavior can be profitably reused, in part because a small number of instances
- 10 can be reused often.

The profiling mechanism described herein is also applicable for selecting load instructions for reuse. Some instructions load values from different addresses. Each value loaded from each location is referred to as a “location-value.” When a load instruction consistently accesses a small number of location-values, the load

15 instruction may be profitably included within a reuse region. The profiling mechanism described herein can be used to profile location-values in a manner similar to that used for profiling set-values as described above. From the profile for location-values, an estimate can be generated for the likelihood that load values will be overwritten by stores.

20 Figure 1 shows a candidate reuse region. A candidate reuse region is a region that can be made into a computation reuse region, but may or may not be a “good” computation reuse region. For the purposes of this description, a good computation reuse region is one which produces instances that are reused often.

Candidate reuse region 100 is shown having multiple instructions, including
25 instructions 104, 106, and 108. Instructions 104 and 108 have registers one and two (r1 and r2) as operands. Likewise, instruction 106 has registers three and four (r3 and r4) as operands. Input registers 102 are shown above candidate reuse region 100 to show that registers r1, r2, and r3 are inputs to the region.

Candidate reuse region 100 has registers 102 as input registers because the
30 first two instructions (instructions 104 and 106) depend upon values held in the input

registers, and the input register values are undisturbed before being used within the region. Regions with small numbers of inputs and outputs are selected as candidate reuse regions.

- A candidate reuse region 100 can also include loop constructs. Software
- 5 loops can be identified as candidate reuse regions when they have small numbers of input and output registers. For ease of explanation, candidate reuse region 100 is not shown as a loop, but rather is shown as a linear sequence of instructions. Input registers 102 are the “input set” to candidate reuse region 100.

- Figure 2 shows individual input values and set-values for the candidate reuse
10 region of Figure 1. Table 200 shows top-values for input register r1 in column 202, top-values for input register r2 in column 204, and top-values for input register r3 in column 206. The term "top-values" as used herein refers to values that occur most frequently. For example, in table 200, value v11 occurs most frequently in input register r1 at the beginning of candidate reuse region 100. Likewise, value v21
15 occurs most frequently in input register r2, and value v31 occurs most frequently in input register r3. Each of columns 202, 204, and 206 show individual top-values for each of input registers r1, r2, and r3 at the beginning of candidate reuse region 100.

- Column 208 shows top set-values for the input set. In this example, the input set consists of input registers 102 (Figure 1). As can be seen in column 208, the top
20 set-value corresponds to the combination of individual values for each input register. For example, the top set-value corresponds to a value of v11 in input register r1, a value of v21 in input register r2, and a value of v31 in input register r3. As can also be seen in column 208, the next most frequently occurring top set-value includes a mix of individual top-values. For example, the next most frequently occurring top
25 set-value corresponds to a value of v11 in input register r1, a value of v22 in input register r2, and a value of v33 in input register r3.

- As previously described, if a small number of top set-values account for a majority of the set-values at the beginning of a candidate reuse region, the candidate reuse region is a good choice for forming a computation reuse region. Individual
30 top-values, such as those shown in columns 202, 204, and 206 do not map directly to

top set-values as shown in column 208. The method and apparatus of the present invention directly profiles top set-values such as those shown in column 208. As a result, candidate reuse regions, such as candidate reuse region 100 (Figure 1) can be selected as computation reuse regions when profitable.

5 Figure 3A shows a set-value in accordance with one embodiment of the invention. Set-value 300 includes three values that correspond to values in three input registers to a candidate reuse region. V1 302, v2 304, and v3 306 are concatenated to produce set-value 300. Set-value 300, as shown in Figure 3A, does not include register names because register names can be inferred from the relative
10 placement of values 302, 304, and 306.

The size of set-value 300 is equal to the sum of the sizes of values 302, 304, and 306. As the number of input registers increases, the size of set-value 300 also increases. As the size of set-value 300 increases, the storage requirements for profiling a large number of candidate reuse regions can become large.

15 Figure 3B shows a set-value in accordance with another embodiment of the invention. Embodiment 350 shows set-value 370 generated as a function of value v1 352, value v2 354, and value v3 356. In embodiment 350, value 352 is shown having three segments. Each segment represents a portion of the total value, such as a single byte in a three byte word. Segments of value 352 are combined, or “folded,”
20 using exclusive-or operator 358. Likewise, segments of value v2 are folded using exclusive-or operator 360, and segments of value 356 are folded using exclusive-or operator 362. The output of exclusive-or operators 358, 360, and 362 are concatenated to produce set-value 370. Set-value 370 represents the combination of the values of the input set of a candidate reuse region. Unlike set-value 300 (Figure
25 3A), set-value 370 does not necessarily grow in size as the number of values increases. For example, if the number of values increases beyond three, additional exclusive-or operators can be employed to combine the additional values prior to concatenation into set-value 370.

Set-value 370 may not be unique for each possible combination of values
30 352, 354, and 356. For example, two different combinations of values may produce

the same set-value 370. This can decrease the accuracy of the resulting profile generated; however, the degraded accuracy is traded for increased storage efficiency. In practice, most profiled values are small, and the likelihood that two profiled input sets result in the same set-value 370 is small. For example, if each of values 352, 5 354, and 356 only have non-zero values in the left-most segment, then no data is lost as a result of the exclusive-or folding operations, and each set-value will be unique.

Set-value 370 is shown in Figure 3B as being generated from values folded using exclusive-or operators. One skilled in the art will understand that other mechanisms exist for folding and combining multiple values into set-value 370.

- 10 10 When exclusive-or operators or other mechanisms are employed, multiple values are combined into a single value, shown as set-value 370 in Figure 3B.

In some embodiments, exclusive-or operators 358 and 360 are implemented in hardware. In some hardware implementations, registers internal to a processor drive exclusive-or circuits that create set-values, such as set-value 370. In other 15 embodiments, exclusive-or operators 358 and 360 are implemented in software. In some software implementations, exclusive-or operators 358 and 360 appear as exclusive-or machine instructions inserted into the software as instrumenting code.

- 15 In general, N input values can be combined into a set-value that is less than N input words long. The combining techniques shown in Figures 3A and 3B can be 20 utilized together or with other combining mechanisms while still practicing the present invention. For example, a subset of the total number of values can be folded using exclusive-or operators resulting in multiple subset-values, which can then be concatenated as shown in Figure 3A to form set-values. Once a set-value is created, any suitable value profiling technique can be used to produce profiling information 25 such as that shown and described with reference to Figure 4 below.

Figure 4 shows a profiling data structure for a candidate region. Profiling data structure 400 includes top set-values 410 and profile indicators 420 arranged in records, and the total number of set-values 430. Record 422 has a set-value shown as "A," and has a profile indicator value of 800. Likewise, record 424 has a set-value 30 shown as "B," and has a profile indicator value of 400. Set-values 410 are shown in

Figure 4 having alphanumeric values for ease of explanation. In some embodiments, set-values 410 have values that include concatenated register values, such as set-value 300 (Figure 3A). In other embodiments, set-values 410 have values corresponding to combined register values, such as set-value 370 (Figure 3B). The 5 total number of set-values 430 is the sum of all the set-values encountered by the profiler at the region entry, including the top set-values and the less frequently encountered set-values.

In the embodiment of Figure 4, profiling data structure 400 is shown in a state existing after a region has been profiled. Top set-values 410 have been profiled, 10 and profile indicators 420 show how often each of top set-values 410 was encountered. For example, as shown in record 422, top set-value A occurred 800 times. Likewise, as shown in record 424, set-value B occurred 400 times. The total number of set-values 430 is equal to 3000. Five hundred of the 3000 sampled set-values did not match set-values in profiling data structure 400 and were discarded.

15 During profiling, when a particular set-value is encountered, profiling data structure 400 is accessed as a function of set-values and the corresponding profile indicator is updated. In this example, the profiling indicator is updated using an increment operation. Profiling data structure 400 only keeps a small number of distinct set-values. For example, profiling data structure 400 may include only eight 20 entries.

The relative probability of occurrence of each top set-value 410 is a function of the total number of set-values 430 collected from the region during profiling. For example, the sum of all profile indicators 420 maintained in data structure 400 is equal to 2500. If the input set of the candidate reuse region were sampled a total of 25 3000 times resulting in profiling data structure 400, the candidate reuse region may be a good candidate for a computation reuse region. The candidate reuse region may be a good computation reuse region in part because the top eight set-values as shown in data structure 400 account for greater than 80 percent ($2500/3000 > .8$) of all set-values sampled for the candidate reuse region.

If, however, profiling data structure 400 results after sampling the input register set a total of 20000 times, the candidate reuse region may not be a good choice for a computation reuse region. The candidate reuse region may not be a good computation reuse region in part because the top eight values as shown in data structure 400 account for less than 13 percent ($2500/20000 < .13$) of all set-values sampled for the candidate reuse region.

In some embodiments, the number of top set-values to profile is a decision made prior to profiling the software. The size of profiling data structure 400 is then set accordingly. If a processor that will ultimately execute the computation reuse regions in the end-user environment has the capability to store a large number of computation reuse instances, then the number of top set-values profiled can also be large. In some embodiments, the size of profiling data structure 400 is at least as large as the number of expected reuse instances that will be stored in the end-user environment.

Profiling data structure 400 can be implemented in any suitable type of physical data structure. In some embodiments, data structure 400 is an array sequentially searched by the set-value. In other embodiments, data structure 400 is implemented in a hash table. In still other embodiments, data structure 400 is a dedicated hardware buffer resident within the processor that performs the profiling operations.

Figure 5A shows a sampling value profiler. As previously described, a good computation reuse region can be selected based on the frequency of occurrence of top set-values. The frequency of occurrence of top set-values can be ascertained by statistically sampling a sufficient number of set-values without sampling every single one. As shown in embodiment 500, value profiler 506 receives one of every "S" set-values from filter 504. Filter 504 receives a set-value 502 each time a candidate reuse region is encountered during profiling, but only passes one of every S set-values to value profiler 506. By sampling every S values, an approximation of the probability of occurrence of top set-values is generated. Figure 5A shows the

sampling mechanism in schematic form. Figure 5B shows an embodiment of a sampling profiler using pseudo-code.

Figure 5B shows instrumenting code that implements the sampling value profiler of Figure 5A. Instrumenting code 520 shows four instructions. In some 5 embodiments, instrumenting code is inserted in a program being profiled at the beginning of a candidate reuse region. Instruction 522 sets one of two predicate registers to "true" and the other to "false" based on the outcome of a "compare" operation. The two predicate registers include a "true" predicate register shown as "pt," and a "false" predicate register shown as "pf." When, in instruction 522, the 10 variable labeled "counter" is equal to zero, the true predicate register is set, and instructions 526 and 528 executed. The execution of instruction 526 results in the counter variable being reinitialized to the sampling interval "S," and the execution of instruction 528 results in a set-value "V₁" being profiled using a profiling function labeled "value_profile." Conversely, if the variable labeled "counter" is not equal to 15 zero, the false predicate register is set, and instruction 524 executes. Each time instruction 524 executes, the counter is decremented.

In some embodiments, much of the code shown in Figure 5B can be shared by multiple candidate regions if it is known that the regions will be entered under the same condition. In other words, if the entries of the regions are control equivalent. 20 For example, instructions 522, 524, and 526 can be placed anywhere prior to control equivalent candidate region entries and candidate load instructions. Instruction 528 can be inserted at each of the control equivalent candidate region entries and candidate load instructions. In these embodiments, instructions 522, 524, and 526 are not repeated for each control equivalent candidate region entry and candidate 25 load instruction. Profiling instructions inserted for profiling each of the control equivalent candidate region entries and candidate load instructions are predicated on the same predicate register.

The value of "S" in Figures 5A and 5B is chosen so that a statistically valid number of samples is collected. For example, if a candidate reuse region is 30 encountered one million times, and the top eight set-values are to be profiled, a few

hundred samples may be sufficient. In this example, S can be set on the order of ten thousand. On the other hand, if a candidate reuse region is encountered only a few hundred times, a statistically valid number of samples should not be too small, and S can be set smaller accordingly.

- 5 In some embodiments, S is set such that a minimum number of samples equal to a multiple of the number of top set-values to be collected during profiling. One such embodiment is shown in the pseudo-code that follows.

```
S = user selected sampling interval  
10      num_samples = region_entry_freq/S  
          min_num_samples = K * num_top_set_values  
          if (num_samples < min_num_samples)  
              S = region_entry_freq/min_num_samples
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- 15 In the example embodiment shown in pseudo-code above, num_samples is the number of set-value samples to be taken, and is initially computed as the total number of occurrences divided by the initial sample interval, S. A minimum number of samples is computed as K times the number of top set-values to be profiled, and if the number of samples previously computed is less than the minimum, the sample 20 interval S is recomputed to satisfy the criteria. In some embodiments, K is greater than or equal to ten.

Embodiments described thus far are generally directed to set-values that can aid in the identification of good computation reuse regions. The method and apparatus of the present invention can also be utilized for profiling location-values 25 that can aid in the identification of good load and store instructions for inclusion in reuse regions. In general, for computation reuse regions, an assumption is made that inputs to the computation reuse region are sourced from registers. Load and store instructions reference values in memory locations. This is described in more detail with reference to Figures 6A-6D below.

Figure 6A shows software instructions that access an array. Embodiment 600 shows software instructions in an end-user program that include a load instruction. The load instruction occurs when the array access is made shown as "a[i]" in Figure 6A. In instruction 602, a variable "x" is initialized to zero. Instruction 604 is the 5 beginning of a "for" loop, and instruction 608 is the end of the "for" loop. Instruction 606 is executed "M" times within the "for" loop.

Instruction 606 can be a good reuse instruction if a small number of top location-values account for a majority of the memory loads. For example, if the 10 array "a" is invariant, each time a particular location within the array is accessed, the value retrieved will be the same. The method and apparatus of the present invention collects top memory locations and top load values as a set. The load location and loaded value is treated as a combined location-value, and the combined location-values are profiled to collect the top location-values for each candidate load or store instruction. At each candidate load instruction, a fixed number of location-values are 15 collected. For example, in some embodiments, 20 location-values are collected for each candidate load instruction.

Figure 6B shows a location-value in accordance with one embodiment of the present invention. Location-value 610 shows location 612 concatenated with value 614. Value 614 is the value loaded from location 612. The combination of location 20 612 and value 614 represent a location-value to be profiled. The concatenation of location 612 and value 614 is similar to the concatenation of values in set-value 300 (Figure 3A).

Figure 6C shows a location-value in accordance with another embodiment of the invention. Figure 6C shows location-value 370 generated as a function of 25 location 612 and value 614. Location 612 is shown having three segments. Each segment represents a portion of the total data word that represents the location, such as a single byte in a three byte word. Segments of location 612 are folded using exclusive-or operator 616. Likewise, segments of value 614 are folded using exclusive-or operator 618. The output of exclusive-or operators 616 and 618 are

concatenated to produce location-value 620. Location-value 620 represents the combination of the location and the value accessed by a candidate load instruction.

Location-value 620 may not be unique for each possible combination of locations 612 and values 614. For example, two different combinations of locations 5 and values may produce the same location-value 620. This can decrease the accuracy of the resulting profile generated; however, the degraded accuracy is traded for increased storage efficiency. In practice, most profiled values are small, and the likelihood that two profiled location-values will result in the same location-value 620 is small. For example, if each of location 612 and value 614 have non-zero values 10 only in the left-most segment, then no data is lost as a result of the exclusive-or operations, and each location-value will be unique.

Location-value 620 is shown in Figure 6C as being generated using exclusive-or operators. One skilled in the art will understand that other mechanisms exist for combining locations and values into location-value 620. When exclusive-or 15 operators or other mechanisms are employed, locations and values are combined into a single value, shown as location-value 620 in Figure 6C.

In some embodiments, exclusive-or operators 616 and 618 are implemented in hardware. In some hardware implementations, registers internal to a processor drive exclusive-or circuits that create location-values, such as location-value 620. In 20 other embodiments, exclusive-or operators 616 and 618 are implemented in software. In some software implementations, exclusive-or operators 616 and 618 appear as exclusive-or machine instructions inserted into the software as instrumenting code.

Figure 6D shows a location-value profiling data structure. Profiling data structure 650 shows location-values 652 and profile indicators 654 arranged in 25 records. Record 656 corresponds to location-value "A," and record 658 corresponds to location-value "B." As is the case with profiling data structure 400 (Figure 4), profile indicators 654 hold the number of times a particular location-value 652 is encountered, and total field 660 includes the total number of times location-values are sampled. When a small number of top location-values represent a large 30 percentage of the location-values for a candidate load instruction, then the candidate

load instruction can be good for computation reuse. In some embodiments, the probability of occurrence of a fixed number of top location-values is compared to a threshold, and if the occurrence probability is higher, the candidate load instruction is selected for inclusion in a computation reuse region.

5 Figure 7 shows a flowchart for a method of selecting reuse regions. Method 700 begins with action 710 when a candidate reuse region is identified within a software program. Candidate reuse regions can be identified using any of a number of criteria. One such candidate reuse region is shown as candidate reuse region 100 in Figure 1.

10 In action 720, the software program code is instrumented for profiling. Instrumenting for profiling includes inserting instructions in the program that profile top set-values and top location-values. In some embodiments, every time a candidate reuse region is encountered, the instrumented code profiles a set-value for the candidate reuse region. In other embodiments, a sampling filter is employed, such as 15 filter 504 (Figure 5A), and only one of every “S” set-values is profiled.

16 In action 730, the instrumented code is executed and the profile data is gathered. As a result, profiling data structures, such as profiling data structure 400 (Figure 4), and profiling data structure 650 (Figure 6D) are generated. In action 740, the probability of occurrence of a top set-value is determined as the ratio of the 20 number of times the top set-value was collected to the total number of times set-values were sampled. When a small number of top set-values represent a large percentage of the execution of the candidate reuse region, then the candidate reuse region will likely make for a good computation reuse region.

21 In action 750, the candidate reuse region is used to form a computation reuse region if appropriate criteria are met. One such criteria is when the probability of occurrence of a small number of top set-values exceeds a threshold. A candidate reuse region can be used by itself or can be combined with other candidate reuse regions to form a computation reuse region.

22 Figure 8 shows a processing system. Processing system 800 includes 30 processor 820 and memory 830. In some embodiments, processor 820 is a processor

capable of executing instrumented software for profiling top set-values and top location-values. Processor 820 can also be a processor capable of selecting good computation reuse regions from candidate reuse regions. Processing system 800 can be a personal computer (PC), mainframe, handheld device, portable computer, set-

- 5 top box, or any other system that includes software.

In some embodiments, processor 820 includes cache memory, a memory controller, or a combination of the two. In these embodiments, processor 820 may access a profile indicator data structure without accessing memory 830. In other embodiments, profile indicators are maintained within memory 830, and processor

10 820 accesses memory 830 when updating profile indicators regardless of whether processor 820 includes cache memory or memory controllers.

Memory 830 can be a random access memory (RAM), read only memory (ROM), flash memory, hard disk, floppy disk, CDROM, or any other type of machine medium readable by processor 820. Memory 830 can store instructions for

15 performing the execution of the various method embodiments of the present invention.

Conclusion

A software profiling mechanism that gathers and profiles top set-values and top location-values has been described. Software to be profiled is instrumented with instructions that sample set-values at the occurrence of candidate reuse regions and sample location-values at the occurrence of candidate load instructions. Set-values and location-values can be generated as concatenated values, or can be combined using mechanisms such as exclusive-or operators. When a small number of top set-values account for a large percentage of occurrences, the candidate reuse region may make a good computation reuse region. Likewise, when a small number of top location-values account for a large percentage of occurrences of candidate load instructions, the candidate load instruction may make a good candidate for inclusion in a computation reuse region.

It is to be understood that the above description is intended to be illustrative, and not restrictive. Many other embodiments will be apparent to those of skill in the art upon reading and understanding the above description. The scope of the invention should, therefore, be determined with reference to the appended claims, 5 along with the full scope of equivalents to which such claims are entitled.